



QUANTUM INFORMATION and COMPUTATION

DRAFT
VERSION

Understanding Quantum Information & Computation

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